

Name: SOLUTIONS (MICAH)

A#:

Section: EF

- [4] 1. If $f(x) = \frac{3x}{x^2 - 2x + 3}$ and $g(x) = x^2 + 1$ then (do not simplify)

$$f(g(x)) = \frac{3(x^2 + 1)}{((x^2 + 1)^2 - 2(x^2 + 1) + 3)}$$

$$g(f(x)) = \left(\frac{-2 - \frac{3x}{x^2 - 2x + 3}}{x^2 - 2x + 3} \right)^2 + 1$$

- [4] 2. Circle equations of lines. (negative points for all wrong circles)

$$3x + 2y + 7 = 0$$

$$y = 4x + \cos x$$

$$y = 3x + \cos(y)$$

$$x = \ln(7)$$

$$5x + (\sin 1)y = 8$$

$$(y - e^3) = -5(x - \tan 3)$$

$$y - 1 = e^y(x^2 - 3)$$

$$xy = 0$$

- [4] 3. State the slope of the line, the x -intercept, the y -intercept, and the slope of any perpendicular line to the line L given by the equation $2x + 3y + 3 = 0$.

$$y = \frac{-2x - 3}{3} = -\frac{2}{3}x - 1$$

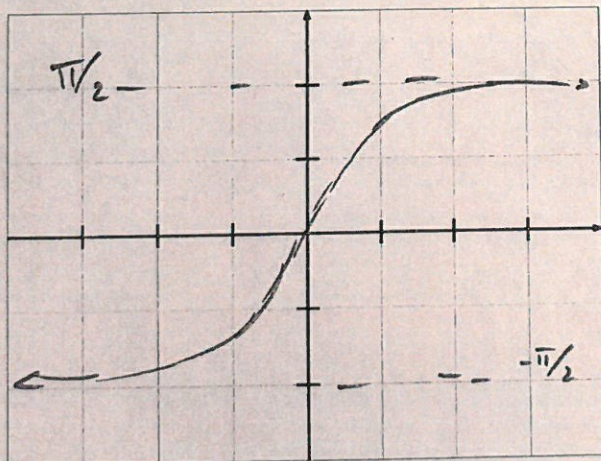
The slope of L is $-\frac{2}{3}$

The x -intercept of L is $-\frac{3}{2}$

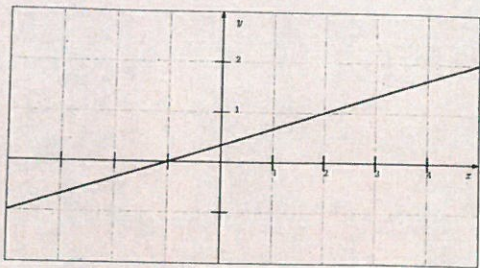
The y -intercept of L is -1

The slope of any line perpendicular to L is $\frac{3}{2}$

- [2] 4. Sketch the graph of $y = \tan^{-1}(x)$ below.



- [2] 5. Find the equation of the line L shown on the graph below.



$$m = 1/3 \text{ (since } (-1, 0) \text{ and } (2, 1) \text{ are on } L)$$

$$y = \frac{1}{3}x + b$$

$$y = \frac{x+1}{3}$$

$$0 = \frac{1}{3}(-1) + b \text{ so } b = \frac{1}{3}$$

equation of L : $y = \frac{1}{3}x + \frac{1}{3}$

- [4] 6. Find the equation of the secant line L of the curve $y = x^3 - 2x - 2$ above the interval $[0, 2]$.
(Recall that a secant line to the curve $y = f(x)$ above the interval $[a, b]$ is the line passing through points $(a, f(a))$, $(b, f(b))$ and usually has no relationship to the sec x function.)

The secant line passes through $(0, f(0) = -2)$ and also

$$(2, f(2) = 8 - 4 - 2 = 2) \text{ Hence its slope } \frac{-2 - 2}{0 - 2} = \frac{-4}{-2} = 2$$

$$\text{so } y = 2x + b$$

$$-2 = 2(0) + b$$

$$b = -2$$

Hence the equation of the secant line is

$$\boxed{y = 2x - 2}$$