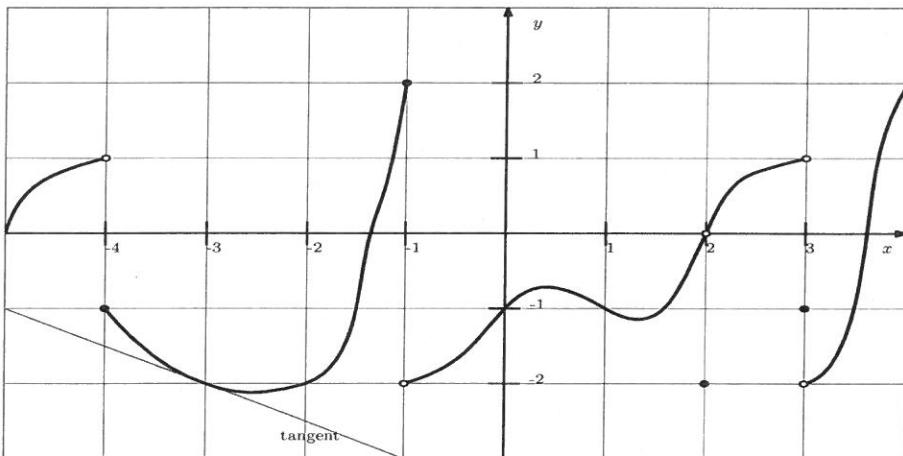


Name: SOLUTION

A#:

Section: A, B

- [9] 1. Let f be a function whose graph of $y = f(x)$ is given below. Compute the following quantities or state that they do not exist.



(a) $f(3) = \underline{-1}$

(b) $\lim_{x \rightarrow 3} f(x) \underline{\text{d.n.e.}}$

(c) $\lim_{x \rightarrow 2} (x^2 + f(x)) \underline{= 4}$

(d) $\lim_{x \rightarrow 1^-} f(x) \underline{=} \text{N/A } -1$

(e) $\lim_{x \rightarrow -1^+} f(x) \underline{=} -2$

(f) $\lim_{x \rightarrow -4^-} e^x f(x) \underline{=} e^{-4}$

(g) The average rate of change of $f(x)$ over the interval $[-3, -1]$ $\underline{= \frac{4}{2}} = \boxed{2}$

(h) The instantaneous rate of change of $f(x)$ when $x = -3$ $\underline{-\frac{1}{2}}$

(i) The equation of the secant line over the interval $[-3, -1]$ $\underline{y + 2 = 2(x + 3)}$

or $\underline{y = 2x + 4}$

[3] 2. Let $f(x) = \begin{cases} x^2 - 1, & \text{if } x < 2 \\ e^{x-2}, & \text{if } x \geq 2 \end{cases}$. Then

$$(a) \lim_{x \rightarrow 2^-} f(x) = \frac{2^2 - 1}{\boxed{3}}$$

$$(b) \lim_{x \rightarrow 1^+} f(x) = \frac{1^2 - 1}{e^{1-2}} = \boxed{0} \quad (\text{and not } e^{1-2} = e^{-1})$$

$$(c) \text{The average rate of change of } f \text{ over the interval } [2, 4] \text{ is } \frac{e^2 - 1}{2}$$

[8] 3. Compute the limit or state that it does not exist.

$$\begin{aligned} (a) \lim_{x \rightarrow -2} \frac{x+2}{\sqrt{x^2+x+2}-2} &= \lim_{x \rightarrow -2} \frac{(x+2)(\sqrt{x^2+x+2}+2)}{(\sqrt{x^2+x+2}+2)(\sqrt{x^2+x+2}-2)} \\ &= \lim_{x \rightarrow -2} \frac{(x+2)(\sqrt{x^2+x+2}+2)}{(x^2+x+2)-4} = \lim_{x \rightarrow -2} \frac{(x+2)(\sqrt{x^2+x+2}+2)}{x^2+x-2} \\ &= \lim_{x \rightarrow -2} \frac{(x+2)(\sqrt{x^2+x+2}+2)}{(x+2)(x-1)} = \lim_{x \rightarrow -2} \frac{\sqrt{x^2+x+2}+2}{x-1} = \frac{\sqrt{(-2)^2-2+2}+2}{-2-1} \\ &= \boxed{-\frac{4}{3}} \end{aligned}$$

can skip these

$$(b) \lim_{x \rightarrow 3^-} \frac{|x-3|}{x^2-x-6} = \lim_{x \rightarrow 3^-} \frac{-(x-3)}{(x-3)(x+2)} = \lim_{x \rightarrow 3^-} \frac{-1}{x+2} = \frac{-1}{3+2} = \boxed{-\frac{1}{5}}$$