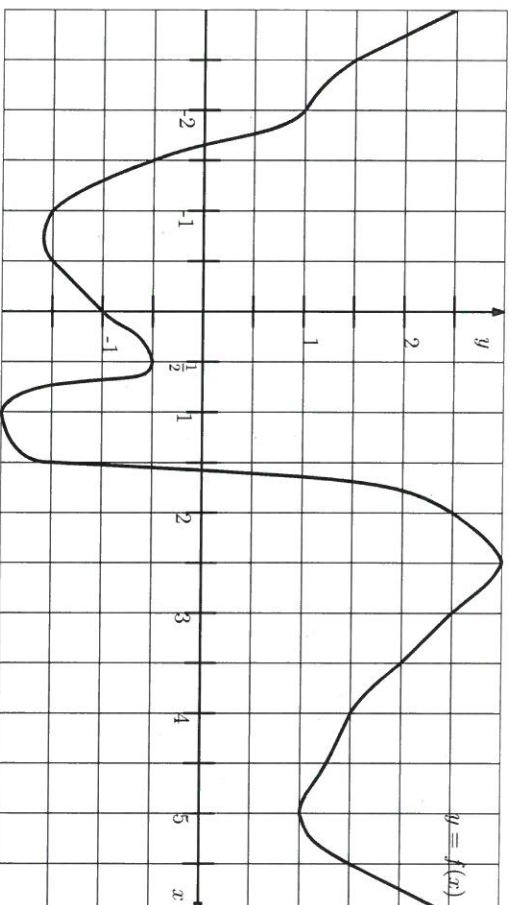


Name: <i>Mil (solutions)</i>	A#:	Section:
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[7]

1. Let f be a function whose graph of $y = f(x)$ is given below. Let L_N and R_N denote the left-endpoint, respectively right end-point, Riemann sums with N subintervals of equal size. Fill in the following.



- (a) Estimate the area under the curve over $[2, 5]$ by L_2 : $\frac{3}{2}(f(2) + f(2.5)) = \frac{3}{2}(-1 + 0) = -\frac{3}{2}$
- (b) Estimate the area under the curve over $[3, 5]$ by R_4 : $\frac{1}{4}(f(3.5) + f(4) + f(4.5) + f(5)) = \frac{1}{4}(1 + 0 + (-1) + 0) = 0$
- (c) Estimate $\int_{-1}^2 f(x) dx$ by L_2 : $\frac{3}{2}(f(-1) + f(1)) = \frac{3}{2}(-1 + 1) = 0$
- (d) Estimate $\int_0^3 (f(\frac{x}{2}) + 1)^2 dx$ by R_3 : $\frac{3}{2}[(f(\frac{3}{2}) + 1)^2 + (f(\frac{3}{2}) + 1)^2 + (f(\frac{3}{2}) + 1)^2] = \frac{3}{2}[0^2 + (-1)^2 + (-1)^2] = 3$
- (e) If $F(x) = \int_0^x f(t) dt$, then $F'(3) = f(3) = 0$
- (f) If $G(x) = \int_{-1}^{x^2} t^2 f(t+1) dt$, then $G'(x) = 2x^2 f(x^2 + 1)$
and $G'(2) = 64 f(5) = 64$

[4] 2. Solve the initial value problem $\frac{dy}{dx} = 3e^{2x}$, $y(0) = 5$.

$$y' = \int 3e^{2x} dx = \frac{3e^{2x}}{2} + C$$

$$y(0) = \frac{3}{2} + C = 5 \quad \text{so } C = 5 - 3/2 = 7/2$$

$$\text{Hence } y = \frac{3e^{2x}}{2} + \frac{7}{2}$$

3. Compute the integral.

[5] (a) $\int (\sin(3x) + \frac{2}{1+x^2} + \sec^2(3x) + e^3 + x^{-3}) dx$

$$= \frac{-\cos(3x)}{3} + 2 \tan^{-1} x + \frac{\tan 3x}{3} + e^3 x - \frac{x^{-2}}{2}$$

[4] (b) $\int_1^3 \frac{1+t^2}{t} dt = \int_1^3 (t^{-1} + t) dt = \left(\ln t + \frac{t^2}{2} \right) \Big|_1^3$

$$= \ln 3 + \frac{9}{2} - \ln 1 - \frac{1}{2} = \ln 3 - 4$$