

Name: SOLUTIONS

A#:

Section:

1. Compute $\int \left(\frac{3}{x} - \frac{x}{4} + 5 \right) dx$

$$= 3 \int \frac{1}{x} dx - \frac{1}{4} \int x dx + \int 5 dx$$

$$= \boxed{3 \ln|x| - \frac{1}{8} x^2 + 5x + C}$$

2. Find all functions $f(x)$ that satisfy $f'(x) = \sqrt{x} - e^x$ and $f(0) = 1$.

$$\begin{aligned} f(x) &= \int (\sqrt{x} - e^x) dx \\ &= \frac{2}{3} x^{3/2} - e^x + C \end{aligned}$$

$$\text{Since } f(0) = 1 \text{ get } 1 = \frac{2}{3}(0)^{3/2} - e^0 + C$$

$$\Rightarrow 1 = 0 - 1 + C$$

$$\Rightarrow C = 2$$

$$\text{So } \boxed{f(x) = \frac{2}{3} x^{3/2} - e^x + 2}$$